discovering MATHEMATICS (2nd Edition)



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INTRODUCTION

Discovering Mathematics 2nd Edition is a series of textbooks designed for students in secondary schools. It is based on the latest syllabus implemented by the Ministry of Education (MOE) from 2013.

The emphasis of this series is on empowering students to learn mathematics independently and effectively. New materials have been added to enhance the learning experience of students, and enable them to make connections within mathematics, between mathematics and other disciplines, and between mathematics and the real world.

The comprehensive and level-specific textbooks, workbooks and support resources aim to the mathematics teaching and learning experience engaging and meaningful. *Discovering Mathematics 2nd Edition* is also the best-selling mathematics textbook series in Singapore.

MATHEMATICS

Concept Development

Chapter Opener

Each chapter begins with an opener, illustrating the concept by establishing a connection between the topic and real-life scenarios. Learning objectives for each chapter are also provided.

Class Activities

Learning through exploration and discovery is emphasized as students are prompted with questions in order to explore the formulation of a concept through class activities. It also fosters group discussions and enriches the overall learning experience for students.

Examples and Try It!

Worked examples demonstrate problem-solving methods and provides sequential guides towards the application of learnt concepts to show how ideas and reasoning can be expressed clearly in mathematical language. A Try It! feature, similarly fashioned after each worked example, is provided to allow students to assess their understanding of the concept(s).

Exercises

Exercises are provided after each section of every chapter within the book. They are sequenced into three levels of difficulty in order to encourage students to think analytically, reason and communicate effectively in mathematical language. A revision exercise is also included at the end of every chapter for students to revise the concepts taught, and to consolidate their learning.



The Authors

Chow Wai Keung, BSc (Hons), Cert.Ed., M.Soc.Sc. (Applied Statistics)

Chow Wai Keung is an established author and an experienced teacher. He has devoted much of his time to writing a wide variety of mathematics textbooks for use in the region. His expertise in mathematics and his enthusiasm in teaching the subject are reflected in his works. His books seek not only to explain complex mathematical concepts but also to provide practical examples, relevant activities and questions to help maximize students' potential

Chin Yeow Chong, BSc (Computer Science), MA (Instructional Design and Technology), PGDE

Chin Yeow Chong has more than 10 years of teaching experience in secondary schools. He is currently teaching Mathematics and Computer Studies at a local international school. His aim for the book is to make the learning of mathematics relevant and practical through the applications of mathematical concepts in solving problems in real-world contexts.

Yong Fook Meng, B.Soc. Sci. (Hons), PGDE

Yong Fook Meng graduated from the National University of Singapore (NUS) as the top student in the Statistics Honours class. He worked as a statistician in the Department of Statistics (DOS), in the Ministry of Trade and Industry (MTI) for three years and taught mathematics in various secondary schools for eight years. An experienced teacher and statistician, as well as a dedicated mathematics educator, Yong Fook Meng introduces a new perspective to the workbooks.

The Consultant

Professor Ling San, BA, MA, PhD (Mathematics) Professor Ling San is a Professor of Mathematical Sciences at Nanyang Technological University (NTU). Previously the Founding Head of the Division of Mathematical Sciences at NTU, he is currently Dean of its College of Science. He was one of only nine distinguished scientists to be conferred the prestigious Singapore National Academy of Science (SNAS) Fellowships. His key areas of research include applications of number theory to coding and cryptography. Professor Ling San is also currently President of the Singapore Mathematical Society.

The General Editor

Ann Lui Yin Leng, BSc, FPDE, Dip. Ed

Ann Lui Yin Leng has more than 25 years of experience in secondary education in Singapore, of which, 22 years were spent in school leadership and mathematics department management. She also has experience across a wide spectrum of secondary schools and academic streams, along with more than 10 years of experience reviewing textbooks in the education service.

The Publisher

Star Publishing Pte Ltd was established in Singapore in 2002. Our field of expertise includes publishing, marketing and distributing educational books and materials in Singapore, Brunei, China and Southeast Asia. Textbook publishing is the company's core business. We have an extensive list of textbooks and educational materials covering a wide range of subjects that are in line with the latest teaching methods. Quality content, innovative designs and high editorial standards form the backbone of the company's values. Our aim is to present and deliver a highly effective learning and teaching experience for both educators and learners with our educational materials. **EXTBOOK FEATURES**



Chapter Opener

- Introduces a chapter through a real-world context and identifies the learning outcomes.
- Videos are available in the Digital Book.

Maths Web

Website references are provided to help students gather information about the concepts discussed.

On the other hand, the range is not always a good measure of spread because it is easily	A
afficeed by the extense values (the larget and multies values) of a data suc. In addition, the range does not show how the data in a set varies between the largest and the smallest values. In this section, we will leave such remeasure of special called standard deviation which takes into account all the values in a data set.	Range, interquartile range and standard deviation are measures of spread of data. Can you compa the advantages among the disadvantages among the
For the data set A mentioned earlier, the mean of the data set is	
$\overline{x} = \frac{13 + 14 + 15 + 18 + 19 + 22 + 25}{7}$	
- 18 We conside the deviations, $s - \xi$, of each kires, s_i of the data set from the nexus. The daggest back objects the deviations of all the terms of a set A from the nexus. Found call have used to set A then the mass of A is a free A is the free A is	We use the notation T is denote the mean of the or x_i, x_j, \dots, x_d i.e. $\overline{x} = \frac{x_i + x_d + \dots + x_d}{N}$
the deviation of 14 from the mean $= 14 - 18 = -4$, : : : : : : : : : : : : :	REMARK
Hence, the deviations are -5, -4, -3, 0, 1, 4 and 7 respectively.	We choose the deviation
Initially, we may think the mean of all these deviations can be a measure of spread. However, the mean of all the deviations = $\frac{-5+(-4)+(-3)+0+1+4+7}{7}$. = 0.	from the mean instead o the deviations from the median or mode. This is because the manipulatio of formulae involving me is easier.
We can overcome this problem by squaring each deviation and then take the mean.	
Thus, the proposed measure of spread = $\frac{(-5)^2 + (-4)^2 + (-3)^2 + 0^2 + 1^2 + 4^2 + 7^2}{7}$	
$=\frac{116}{7}$.	
This measure is the up (new). However, the unit of this measure is the square of the original unit. If the suit of the signal data is sing or doils. This sensature would have the orderend unit light or delite." In order to have a measure of operand with the same unit as the original data, we take the square root of the above expression, $\sqrt{\underline{1000}} = 4.07$ (correct to 3.4 L)	

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Recall

Helps students to recall important mathematical concepts and definitions covered previously and relate them to the current topic.

Remark

Highlights important learning points in the right margin of the textbooks whenever appropriate.

Discuss

Encourages teachers and students to engage in meaningful classroom interaction by posing thought-provoking questions related to the concepts learnt.



Maths Matter

- $\frac{\Sigma h^2}{\Sigma f} = \left(\frac{\Sigma h}{\Sigma f} \right)$ $=\sqrt{\frac{39850}{50}} \cdot \left(\frac{1270}{50}\right)^2$ = \$12.22 (constant) $< t \le 2$ $2 < t \le 4$ $4 < t \le 6$ $6 < t \le 8$ $8 < t \le 1$ 11 18 15 9 7
- Enriches the learning process with interesting and fascinating facts related to mathematics.

Examples & Try It!

- Provides worked examples to demonstrate the ideas and reasoning behind the concepts as well as facilitate students' understanding.
- Includes a similar question i.e. Try it! for students to practise and find out how well they have grasped the concepts.



Graded Exercises

- Consists of questions with 3 levels of difficulty
 - Level 1 Straightforward questions involving direct application of concepts
 - Level 2 More challenging questions involving direct application of concepts
 - *Level 3* Questions involving real-life applications, thinking skills and open-ended answers

Class Activities

 Hands-on activities for students to learn mathematical concepts through exploration and discovery.

Problem-solving Processes & Heuristics

 Provides a list of general processes and heuristics used in problem-solving.

Review Exercises

 Integrates questions after several chapters to reinforce students' mastery of the concepts they have previously learnt.

Problems in Real-World Contexts

 Connects mathematical learning with real-world problems by getting students to understand the real-world situations and devise mathematical models to solve them. This enables students to interpret their solution, opening their minds to a deeper understanding of mathematics and its real world applications.



Go Further

 Provides students with more challenging questions and extends their mastery of the subject.

Local Bits

 Cultivates within students a sense of belonging to Singapore by infusing local contexts within the content and questions.

2 High		
In a	Standard Deviation for Ungrouped Data	Gel 12
	Definition: Standard deviation = $\sqrt{\frac{\Sigma(x-2)}{N}}$	1008
	where $\overline{x} = mean = \frac{\Sigma_{x}}{N}$	2.6%
	and $N = \text{total number of observations.}$	C-109
	formula: Standard deviation = $\sqrt{\frac{\Sigma x^2}{N} - (\frac{\Sigma x}{N})^2}$	1.12
	When the ungrouped data is in a frequency table,	100 A
	mean = $\frac{1}{\Sigma f}$	16825
	standard deviation = $\sqrt{\frac{2f(x-x)}{2f}}$	1. S. 19
11 10 10		10 Car 12 A
	Standard Deviation for Grouped Data	1000
	Definition: Estimated standard deviation = $\frac{1}{2 f(x-x)}$	2000
	where $\overline{x} = \text{estimated mean} = \frac{\sum_{j=1}^{N}}{\sqrt{\pi}}$	1115
	and $\Sigma f = N = \text{total number of observations}.$	12.652
	formula: Estimated standard deviation = $\sqrt{\frac{\Sigma \dot{\mu}^2}{\Sigma f} \cdot \left(\frac{\Sigma \dot{\mu}}{\Sigma f}\right)^2}$	100
1000	Local Social Local Social S	100 1 . Al 7.
	Using Mean and Standard Deviation to Compare Two S	ets of Data
	 Higher mean indicates higher average value of the data set. Higher standard deviation indicates 	10.007
	 wider spread of data Invert consistency of data 	10.05
	 higher variability of data 	6020
		1.10

Flashback

 Recalls previously learnt mathematical concepts for students to build on in the current topic.



Summative Assessment Questions

These questions assess students on the application of mathematical concepts, the interpretation of the contexts, problem-solving skills, and the ability to justify and reason with mathematical concepts. These questions have been carefully crafted to assess students' ability to provide qualitative answers, sometimes applying two or more concepts to solve a problem. Gaining positive ground in examinations, summative assessment questions would greatly assist in preparing students for examinations.



Questions With Real-World Contexts

These questions are designed to convey to students the relevance of mathematics in familiar real-life situations. Students will be guided on how to apply mathematical knowledge obtained from these problems, thus enabling them to gain new perspectives on how mathematics affects the world around them.



Revision Topics

Revision topics are a comprehensive end-syllabus package consisting of integrated examples and revision practice. These components work in tandem to help students recap key concepts and methods, make connections between different topics and ultimately reinforce their mathematical concepts and skills through practice.

3.3 Multiplication of Probabilities

A Independent Events

Two events are said to be **independent events** when the occurrence or non-occurrence of one event will not affect the probability of occurrence of the other event.

For example, in tossing a fair coin twice, the event *A* that the first toss shows a head and the event *B* that the second toss shows a head are independent. That is, event *A* does not affect how likely event *B* will occur, and vice versa.

On the other hand, if the occurrence or non-occurrence of an event affects the occurrence of another event, then these two events are said to be **dependent events**.

For example, in tossing a fair coin twice, the event C that the first toss is a tail and the event D that both tosses are tail are dependent events. This is because the occurrence of event C determines the occurrence of event D.

CLASS ACTIVITY 3

Objectives: To discuss and differentiate between independent events and dependent events.

- 1. A red six-sided die and a green six-sided die are rolled.
 - Let *A* be the event that the red die shows a 3, *B* be the event that the green die shows a 6,
 - *C* be the event that the sum of both dice is 9.

Determine whether each of the following pair of events is independent or dependent. Explain your answer.

- (a) A and B
- **(b)** *A* and *C*
- (c) *B* and *C*
- 2. Two students are selected at random from a class.
 - Let P be the event that the height of the first student is above 170 cm, Q be the event that the heights of both students are above 170 cm,
 - R be the event that the height of the second student is below 165 cm.

Determine whether each of the following pair of events is independent or dependent. Explain your answer.

- (a) P and Q
- (**b**) *P* and *R*
- (c) *Q* and *R*
- 3. Give an example of two independent events in an experiment.

4. Give an example of two dependent events in an experiment.

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SUPPORT RESOURCES

Teacher's Editions

MATHEMATICS (18)

MATHEMATICS (A)

Include answers printed in red for all exercise questions to facilitate teachers to view the answers at a glance.

THEMATICS (

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ATHEMATICS



Teacher's Guides

eacher's Edition

Consist of

Scheme of Work

Assist with lesson planning by cross-referencing lesson objectives with relevant activities and resources.

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MATHEMATICS

- Notes on Teaching
 Suggest teaching approaches to each chapter and section.
- *Fully Worked Solutions* Include both questions and detailed answers for all exercises in the textbooks.

Online Resources

Consist of

- Classroom Printable Worksheets
- Specimen Test Papers for mid-year and end-of-year examinations
- Examination Type Questions





Workbooks

The workbooks supplement the textbooks by providing students with more opportunities to practice and reinforce the concepts learnt.



DIGITAL BOOK

The Digital Book is a complete library of electronic resources that brings the whole lesson together in one platform. Based on the printed textbook, it provides support that gives teachers access to electronic resources and add their own teaching notes.

The Digital Book includes the digital version of the textbook, animations, video clips, worked solutions and step-by-step video guide for solving problems. In addition, there are hundreds of differentiated questions to cater for students of various learning abilities, ensuring ample practice for all students. Fully worked solutions are provided for parents and teachers to check the answers conveniently.

- Extraction/ Zooming Function in Textbook content
- Video chapter openers
- Fully worked solutions for all exercises
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- Embedded calculator for instant use
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- Drawing pen for user to write freely on any part of the Digital Book



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